

# EDL Capacitance

## EDL Capacitance in Water

Calculating the actual capacitance of a water fuel cell requires understanding how the Electric Double Layer contributes to the total capacitance. This page explains how to account for EDL effects in your VIC circuit calculations.

## Total WFC Capacitance Model

The total capacitance of a water fuel cell is not simply the geometric parallel-plate capacitance. It includes contributions from multiple components:

### Series Combination of Capacitances:

$$1/C_{\text{total}} = 1/C_{\text{geo}} + 1/C_{\text{edl,anode}} + 1/C_{\text{edl,cathode}}$$

Where:

- $C_{\text{geo}}$  = geometric (parallel-plate) capacitance
- $C_{\text{edl,anode}}$  = double layer capacitance at anode
- $C_{\text{edl,cathode}}$  = double layer capacitance at cathode

## Geometric Capacitance

The geometric capacitance depends on electrode geometry and water's dielectric constant:

### For Parallel Plate Electrodes:

$$C_{\text{geo}} = \epsilon_r \times A / d$$

Where  $\epsilon_r \approx 80$  for water at room temperature

### For Concentric Tube Electrodes:

$$C_{\text{geo}} = (2\pi \times \epsilon_r \times L) / \ln(r_{\text{outer}}/r_{\text{inner}})$$

Where L is the tube length, r is the radius

# EDL Capacitance Density

The EDL capacitance is typically specified per unit area:

Electrode Material	$C_{\text{dl}}$ ( $\mu\text{F}/\text{cm}^2$ )	Notes
Stainless Steel 316	20-40	Common WFC electrode
Stainless Steel 304	15-35	Also commonly used
Platinum	25-50	High catalytic activity
Graphite/Carbon	10-20	Lower EDL capacitance
Titanium	30-60	Oxide layer affects value

# Calculating Total EDL Capacitance

EDL Capacitance for an Electrode:

$$C_{\text{edl}} = c_{\text{dl}} \times A$$

Where:

- $c_{\text{dl}}$  = specific EDL capacitance ( $\mu\text{F}/\text{cm}^2$ )
- A = electrode surface area ( $\text{cm}^2$ )

# Example Calculation

Given:

- Electrode area: 100 cm<sup>2</sup>
- Electrode gap: 1 mm
- $c_{dl}$ : 25  $\mu\text{F}/\text{cm}^2$  (for stainless steel)

### Calculate:

*Geometric capacitance:*

$$C_{\text{geo}} = (8.854 \times 10^{-12} \times 80 \times 0.01) / 0.001 = 7.08 \text{ nF}$$

*EDL capacitance per electrode:*

$$C_{\text{edl}} = 25 \mu\text{F}/\text{cm}^2 \times 100 \text{ cm}^2 = 2500 \mu\text{F} = 2.5 \text{ mF}$$

*Total capacitance:*

$$1/C_{\text{total}} = 1/7.08\text{nF} + 1/2.5\text{mF} + 1/2.5\text{mF}$$

$$C_{\text{total}} \approx 7.08 \text{ nF} \text{ (EDL contribution is negligible when } C_{\text{edl}} \gg C_{\text{geo}})$$

## When EDL Matters Most

The EDL capacitance becomes significant when:

Condition	EDL Impact	Reason
Very small electrode gap	Minimal	$C_{\text{geo}}$ becomes very large
Large electrode gap (>5mm)	Minimal	$C_{\text{geo}}$ is small, dominates total
Small electrode area	Significant	$C_{\text{edl}}$ becomes comparable to $C_{\text{geo}}$
High frequency operation	Significant	EDL may not fully form

## Frequency Dependence

The EDL capacitance is not constant with frequency:

- **Low frequency (<100 Hz):** Full EDL capacitance available
- **Medium frequency (100 Hz - 10 kHz):** EDL partially developed
- **High frequency (>10 kHz):** EDL contribution decreases; diffuse layer can't follow

This frequency dependence is modeled using the Cole-Cole relaxation model (covered in Chapter 3).

## Effect of Water Purity

The ionic content of water affects both conductivity and EDL behavior:

Water Type	Conductivity	EDL Thickness	C <sub>dl</sub> Effect
Deionized	<1 μS/cm	~100 nm	Lower C <sub>dl</sub>
Distilled	1-10 μS/cm	~30 nm	Moderate C <sub>dl</sub>
Tap water	200-800 μS/cm	~1 nm	Higher C <sub>dl</sub>
With electrolyte (NaOH, KOH)	>1000 μS/cm	<1 nm	Highest C <sub>dl</sub>

## In the VIC Matrix Calculator

The VIC Matrix Calculator's Water Profile settings account for EDL effects:

- **Electrode material:** Determines specific C<sub>dl</sub>
- **Water conductivity:** Affects EDL thickness and capacitance
- **Temperature:** Influences dielectric constant and ion mobility
- **EDL thickness parameter:** Allows fine-tuning based on measurements

**Practical Tip:** For most VIC calculations using typical electrode gaps (1-3mm), the geometric capacitance dominates. However, for very close electrode spacing or when precise tuning is needed, including EDL effects can improve accuracy.

*Next: The Helmholtz Model →*

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